| Q. no. | Expected solutions | mar |
|--------|---|-----|
| | Section-A | |
| 1 | (b)2 | 1 |
| 2 | (c) rational number | 1 |
| 3 | (c) $\frac{x^2}{2} - \frac{x}{2} - 6$ | 1 |
| 4 | (c) no real roots | 1 |
| 5 | (c)4 | 1 |
| 6 | (a) (0,0) | 1 |
| 7 | (a) 50° | 1 |
| 8 | (a) 50° | 1 |
| 9 | Point of contact | 1 |
| 10 | $\frac{\sqrt{3}}{2}$ | 1 |
| 11 | False | 1 |
| 12 | cos90°= 0 | 1 |
| 13 | (d) $\frac{p}{720} \times 2\pi r^2$ | 1 |
| 14 | 36.67 <i>cm</i> | 1 |
| 15 | (a) 3:7 | 1 |
| 16 | (b) 17.5 | 1 |
| 17 | (b)21 | 1 |
| 18 | (c) 9 | 1 |
| 19 | (c) Assertion(A) is true but Reason(R) is false. | 1 |
| 20 | (a)Both Assertion(A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion(A). | 1 |
| | Section B | |
| 21. | The given system of equation is | |
| | kx+3y-(k-3)=0(i) | |
| | 12x+ky-k=0(ii) | |
| | On comparing with $ax + by + c = 0$, we get | |
| | $a_1 = k, b_1 = 3$ and $c_1 = -(k-3)$ [from (i)] | |
| | $a_2 = 12$, $b_2 = k$ and $c_2 = -k$ [from (ii)] | |
| | For no solution, | |

| $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ | |
|---|-----|
| For no solution, $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ $\Rightarrow \frac{k}{12} = \frac{3}{k} \neq \frac{-(k-3)}{-k}$ | 1/2 |
| Taking first two parts, we get $\frac{k}{12} = \frac{3}{k}$ | |
| $\Rightarrow k^2 = 36$ $\Rightarrow k = \pm 6$ 12 k $\Rightarrow k = \pm 6$ | 1/2 |
| Taking last two parts, we get $\frac{3}{k} \neq \frac{-(k-3)}{-k}$ | |
| $\Rightarrow 3k \neq k(k-3)$ $\Rightarrow 3k - k(k-3) \neq 0$ | |
| $\Rightarrow k(3 - k + 3) \neq 0$ $\Rightarrow k(6 - k) \neq 0$ $\Rightarrow k \neq 0 \text{ and } k \neq 6$ | 1/2 |
| Hence, required value of k for which the given pair of linear equations have no solution is -6. | 1/2 |
| | |
| | |

| OR 21 | By Elimination method: | 1/2 |
|-------|--|-----|
| | Equations are $3x + 4y = 10$ | 1/2 |
| | and 2x - 2y = 2 Multiplying equation (ii) by 2 and adding to equation (i) we | |
| | Multiplying equation (ii) by 2 and adding to equation (i), we $3x + 4y = 10$ | |
| | 4x - 4y = 10 $4x - 4y = 4$ | 1/2 |
| | 7x = 14 | |
| | \Rightarrow $x = 2$ | 1/2 |
| | Now, putting the value of x in equation (i) , we get | |
| | $3(2) + 4y = 10 \Rightarrow 6 + 4y = 10$ | |
| | $\Rightarrow \qquad 4y = 4 \qquad \Rightarrow [y = 1]$ | 1/2 |
| 22 | A C B | |
| | OA . OB = OC . OD (Given) $So_{,\overline{OC}}^{,\overline{OA}} = \frac{OD}{OB}(1)$ | 1/2 |
| | Also, we have \angle AOD = \angle COB (Vertically opposite angles)(2) | 1/2 |
| | Therefore, from (1) and (2), \triangle AOD \sim \triangle COB (SAS similarity criterion) | 1/2 |
| | So, $\angle A = \angle C$ and $\angle D = \angle B$ (Corresponding angles of similar triangles) | 1/2 |
| 23 | Let O be the centre of the concentric circle of radii 5 cm and 3 cm respectively. Let AB be a chord of the larger circle touching the smaller circle at P. | |
| | | |

| | Then | 1/2 |
|-----|---|-----|
| | AP=PB and OP⊥AB | |
| | Applying Pythagoras theorem in $\triangle OPA$, we have $OA^2 = OP^2 + AP^2$ | 1/2 |
| | $\Rightarrow 25 = 9 + AP^2$ | 1/2 |
| | \Rightarrow AP ² =16 \Rightarrow AP=4 cm | |
| | ∴AB=2AP=8 cm | 1/2 |
| 24. | $\sin\theta + \cos\theta = \sqrt{3}$ | |
| | $\Rightarrow (\sin\theta + \cos\theta)^2 = 3$ $\Rightarrow \sin^2\theta + \cos^2\theta + 2\sin\theta\cos\theta = 3$ | 1/2 |
| | \Rightarrow 1+2sin θ cos θ =3 | |
| | $\Rightarrow 2\sin\theta\cos\theta=2$ | 1/2 |
| | ⇒sinθcosθ=1 | |

| | | <u> </u> |
|-------|---|----------|
| | $\Rightarrow \sin\theta\cos\theta = \sin^2\theta + \cos^2\theta$ | 1 /2 |
| | . 2 0 2 0 | 1/2 |
| | $\Rightarrow 1 = \frac{\sin^2 \theta + \cos^2 \theta}{\sin^2 \theta}$ | |
| | $\sin \theta \cos \theta$ | |
| | | |
| | $\Rightarrow \tan\theta + \cot\theta = 1$ | 1/2 |
| OR 24 | $5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ$ | |
| | $\sin^2 30^\circ + \cos^2 30^\circ$ | |
| | $= \frac{5 \times \left(\frac{1}{2}\right)^2 + 4 \times \left(\frac{2}{\sqrt{3}}\right)^2 - 1}{\left(\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2}$ | 1 |
| | $=\frac{\frac{5}{4}+\frac{16}{3}-1}{\frac{1}{4}+\frac{3}{4}}=\frac{67}{12}.$ | 1 |
| 25. | Total area cleaned by 2 wipers | |
| | =2× area cleaned by 1 wiper | 1/2 |
| | =2× area of sector with 115° | |
| | | |
| | | |
| | $=2\times \frac{\theta}{360^{\circ}}\times\pi r^{2}$ | 1/2 |
| | $=2\times\frac{115^{\circ}}{360^{\circ}}\times\frac{22}{7}\times25^{2}$ | 1/2 |
| | Therefore area cleaned by wipers = $\frac{158125}{126}$ = 1254.96 cm ² | 1/2 |
| | Section C | |
| 26. | Let us assume that | |
| | | |

| $3-2\sqrt{5}$ is rational. | 1/2 |
|--|---|
| Hence it can be written in the form | |
| $\frac{a}{b}$ where a and b are co-prime and b $\neq 0$ Hence $3-2\sqrt{5} = \frac{a}{b}$ | 1/2 |
| 27 | 1/2 |
| $\Rightarrow 2\sqrt{5} = 3 - \frac{a}{b} = \frac{3b - a}{b}$ | 1/2 |
| $\Rightarrow \sqrt{5} = \frac{3b - a}{2b}$ | 1/2 |
| where $\sqrt{5}$ is irrational and $\frac{3b-a}{2b}$ is rational. | |
| because irrational number≠ rational number Therefore the above is a contradiction. So our assumption is wrong. | 1/2 |
| Hence $3-2\sqrt{5}$ is irrational. | 1/2 |
| Since α and β are the zeroes of the polynomial $f(x)=5x^2-7x+1$ | |
| $\therefore \alpha + \beta = -\left(\frac{-7}{5}\right) = \frac{7}{5} \text{ and } \alpha\beta = \frac{1}{5}$ | 1 |
| $Now_{\beta}^{\alpha} + \frac{\beta}{\alpha} = \frac{\alpha^2 + \beta^2}{\alpha\beta} = \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta} =$ | 1 |
| | Hence it can be written in the form $\frac{a}{b} \text{where a and b are co-prime and b} \neq 0$ $\text{Hence } 3-2\sqrt{5} = \frac{a}{b}$ $\Rightarrow 2\sqrt{5} = 3 - \frac{a}{b} = \frac{3b-a}{b}$ $\Rightarrow \sqrt{5} = \frac{3b-a}{2b}$ where $\sqrt{5}$ is irrational and $\frac{3b-a}{2b}$ is rational. because irrational number \neq rational number. Therefore the above is a contradiction. So our assumption is wrong. Hence $3-2\sqrt{5}$ is irrational. Since α and β are the zeroes of the polynomial $f(x)=5x^2-7x+1$ $\therefore \alpha+\beta=-\left(\frac{-7}{5}\right)=\frac{7}{5}$ and $\alpha\beta=\frac{1}{5}$ |

| | | $= \frac{\left(\frac{7}{5}\right)^2 - 2 \times \frac{1}{5}}{\frac{1}{5}}$ | |
|----|--|--|------|
| | | $= \frac{\left(\frac{7}{5}\right)^2 - 2 \times \frac{1}{5}}{\frac{1}{5}}$ $= \frac{\frac{49}{25} \cdot \frac{2}{5}}{\frac{1}{5}} = \frac{\frac{49 - 10}{25}}{\frac{1}{5}} = \frac{39}{25} \times 5 = \frac{39}{5}$ | 1 |
| 28 | Given equations | are | |
| | x+3y=6 | | |
| | $\begin{array}{ c c c c c c c c c c c c c c c c c c c$ | 6 | 1/2 |
| | $y=\frac{6-x}{3}$ 2 | 0 | |
| | | | |
| | and | | |
| | 2x-3y=12 | | |
| | | | |
| | x 0 | 3 | 1 /0 |
| | y= -4 | -2 | 1/2 |
| | $\frac{2x-12}{2}$ | _ | |
| | 3 | | |
| | | | |
| | Dlot the area into A | (0, 2), D(6, 0) | |
| | Plot the points A $P(0, -4)$ and $Q(3)$ | | |
| | | the points to form the lines AB and PQ as | |
| | shown in Fig. | r | |
| | _ | | |
| | | there is a point B (6, 0) common to both the | |
| | | So, the solution of the pair of linear $x = 0$, i.e. the given pair of equations | |
| | equations is $x = 6$ is consistent. | 6 and $y = 0$, i.e., the given pair of equations | 1 |
| | 15 COHSISICHT. | | |
| | | | |
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| | | | |
| | | | |

| | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 1 |
|-------|--|------|
| OR 28 | Let the numbers be xand y | |
| | According to given condition, x=3y(i) | 1/2 |
| | | |
| | x-y=26(ii) | 1/2 |
| | | |
| | On solving (i) and (ii) we get, | |
| | x=3y [From (i)] Substituting value of x in (ii) | 1/2 |
| | 3y-y=26 | 1, 2 |
| | 2y=26 | |
| | y=13 | 1/2 |
| | Now, x=3y | |
| | $\begin{array}{c} x=3(13) \\ \Rightarrow x=39 \end{array}$ | 1/2 |
| | ∴y=13,x=39 | |
| | ∴ The required numbers are 13 and 39. | 1/2 |
| 29 | Suppose ∠PTQ=θ Since,"The lengths of tangents drawn from an external point to a circle are equa So, ΔTPQ is an isosceles triangle. | 1/2 |
| | $\therefore \angle TPQ = \angle TQP = \frac{1}{2}(180^{\circ} - \theta) = 90^{\circ} - \frac{\theta}{2}$ | 1/2 |
| | | |

| | $T \longrightarrow Q$ | 1/2 |
|-------|--|-----|
| | Also, The tangents at any point of a circle is perpendicular to the radius through the point of contact" ∠OPT=90° | 1/2 |
| | $\therefore \angle OPQ = \angle OPT - \angle TPQ = 90^{\circ} - (90^{\circ} - \frac{\theta}{2})$ $= \frac{\theta}{2} = \frac{1}{2} \angle PTQ$ | 1/2 |
| | Hence ∠PTQ=2∠OPQ | 1/2 |
| 30 | LHS = $(\cos \theta - \cot \theta)^2$ = $\left(\frac{1}{\sin \theta} - \frac{\cos \theta}{\sin \theta}\right)^2 = \left(\frac{1 - \cos \theta}{\sin \theta}\right)^2$ | 1 |
| | $=\frac{(1-\cos\theta)^2}{\sin^2\theta}=\frac{(1-\cos\theta)^2}{1-\cos^2\theta}$ | 1 |
| | $=\frac{(1-\cos\theta)^2}{(1-\cos\theta)(1+\cos\theta)}=\frac{1-\cos\theta}{1+\cos\theta}=RHS.$ | 1 |
| OR 30 | Consider the length of the ladder = 15 m (Hypotenuse) | |
| | | |
| | | |
| | 1 | |

| From the figure Angle between the ladder and the wall ∠BCA | |
|--|-----------|
| Angle between ladder and the ground ∠CAB We know that | 1/2 |
| BC is the height of the wall $\sin 30^{\circ} = BC/15$ | 1 |
| 1/2 = BC/15 | 1/2 |
| So we get | |
| BC = 15/2 BC = 7.5 m | 1/2 |
| Therefore, the height of the wall is 7.5 m. | |
| We use the basic formula of probability to so Probability = $\frac{\text{Total number of favorable of Number of possible outoff}}{\text{Number of possible outoff}}$ When a coin is tossed three times, the total poare: | omes omes |
| i) Sweta will lose her entry fee if she throw Therefore, the probability that she loses her | |

| | P(TTT)=1/8 | 1 |
|-------|---|-----|
| | ii) Sweta will receive double the entry fee if she throws three heads. Therefore, the probability that she gets double the entry fee = P(HHH)= 1/8 | 1 |
| | (iii) Sweta will get her entry fee back if one or two heads show. | |
| | Therefore, the probability that she gets her entry fee = $P\{HTH,THT,HHT,TTH,HTT,THH\} = \frac{6}{8} = \frac{3}{4}$ | 1 |
| | SECTION D | |
| 32. | Step 1: Find time taken for the journey Let the speed of the train be $x \ kmph$ Time taken for the journey $= \frac{480}{x}$ Given speed is decreased by $8 \ kmph$ Hence the new speed of train $= (x-8) \ kmph$ Time taken for the journey $= \frac{480}{(x-8)}$ Step 2: Find the speed of the train Now according to question $\frac{480}{(x-8)} - \frac{480}{x} = 3$ $\Rightarrow \frac{480(x-x+8)}{x(x-8)} = 3$ $\Rightarrow \frac{480}{x} \times 8 = x^2 - 8x$ | 1 1 |
| | \Rightarrow $1280 = x^2 - 8x$ $x^2 - 8x - 1280 = 0$ On solving we get $x = 40$ Hence, the speed of train is $40 \ kmph$. | 1 |
| OR 32 | Let the first integer number = x Next consecutive positive integer will = x+1 | 1 |

| | Product of both integers = $x \times (x+1) = 306$ | 1/2 |
|-----|---|-----|
| | $x^{2}+x=306$ $\Rightarrow x^{2}+x-306=0$ | 1/2 |
| | $\Rightarrow x^{2}+18x-17x-306=0$ \(\Rightarrow x(x+18)-17(x+18)=0\) \(\Rightarrow (x+18)(x-17)=0\) | 1 |
| | Either x+18=0 or x-17=0 \Rightarrow x=-18 or x=17 | 1 |
| | Since integers are positive x can only be 17 $\therefore x+1=17+1=18$ Therefore, two consecutive positive integers will be 17 and 18. | 1 |
| 33. | Solution: | |
| | Given: In ΔABC, DE BC | 1/2 |
| | D E | |
| | B | 1/2 |
| | To prove: $\frac{AD}{DB} = \frac{AE}{EC}$ | 1/2 |

| Construction: Draw EM⊥AB and DN⊥AC. Join B to E and C to D | 1/2 |
|---|-----|
| Proof: In ΔADE and ΔBDE | |
| $\frac{\text{Area of}\Delta ADE}{\text{Area of }\Delta BDE} = \frac{\frac{1}{2} \times AD \times EM}{\frac{1}{2} \times DB \times EM} = \frac{AD}{DB} (i)$ | 1/2 |
| In $\triangle ADE$ and $\triangle CDE$ $\frac{Area \text{ of } \triangle ADE}{Area \text{ of } \triangle CDE} = \frac{\frac{1}{2} \times AE \times DN}{\frac{1}{2} \times EC \times DN} = \frac{AE}{EC} \qquad(ii)$ | 1/2 |
| Since, DE BC [Given] | |
| $\therefore \text{ ar}(\Delta \text{BDE}) = \text{ar}(\Delta \text{CDE}) (iii)$ [Δs on the same base and between the same parallel sides are equal in area] | 1 |

| | From eq. (i), (ii) and (iii) | 1 |
|-----|--|---|
| | $: \frac{AD}{DB} = \frac{AE}{EC}$ Hence proved. | |
| 34. | 4 m 8 4 m | |
| | Radius of cylinder = 2 m, height = 2.1 m and slant height of conical top = 2.8 m | 1 |
| | Curved surface area of cylindrical portion= $2\pi rh$ = $2\pi \times 2 \times 2.1$ = $8.4\pi m^2$ | 1 |
| | Curved surface area of conical portion= π rl = $\pi \times 2 \times 2.8$ = 5.6π m ² | 1 |
| | Total curved surface area= $8.4\pi+5.6\pi=14\times22/7=44\text{m}^2$ | 1 |
| | Cost of canvas = Rate × Surface area=500×44=Rs.22000 | 1 |

| OR 34 | 2 cm 8 cm | |
|-------|--|----------------|
| | Radius of cylinder = 1 cm, height of cylinder = 8 cm, radius of sphere = 8.5/2cm | 1/2 |
| | Volume of cylinder= π r ² h= π ×(1) ² ×8=8 π cm ³ | $1\frac{1}{2}$ |
| | Volume of sphere = $\frac{4}{3}\pi r^3$ = $\frac{4}{3} \times \pi \times (8.5/2)^3 = 614125/6000 \ \pi \text{cm}^3$ | $1\frac{1}{2}$ |
| | Total volume = Volume of sphere + Volume of cylinder $= (\frac{614125}{6000} + 8)\pi$ $= (\frac{614125 + 48000}{6000})\pi$ $= 346.51 \text{ cm}^{3}$ | 1^1_2 |
| | | |

35.

The cumulative frequencies with their respective class

intervals are as follows.

| Weight (in | Frequency | Cumulative |
|------------|-----------|------------|
| kg) | (f) | frequency |
| | | |
| 40 – 45 | 2 | 2 |
| 40 – 43 | 2 | 2 |
| | | |
| 45-50 | 3 | 5 |
| 50-55 | 8 | 13 |
| | | |
| 55-60 | 6 | 19 |
| 60-65 | 6 | 25 |
| | | |
| 65-70 | 3 | 28 |
| 70-75 | 2 | 30 |
| | | |
| Total(n) | 30 | |
| | | |

Cumulative frequency just greater than $\frac{n}{2}$ (i. e. $\frac{30}{2} = 15$) is 19,

belonging to class interval 55 - 60.

Median class = 55 - 60

.....

.

Lower limit (l) of median class = 55

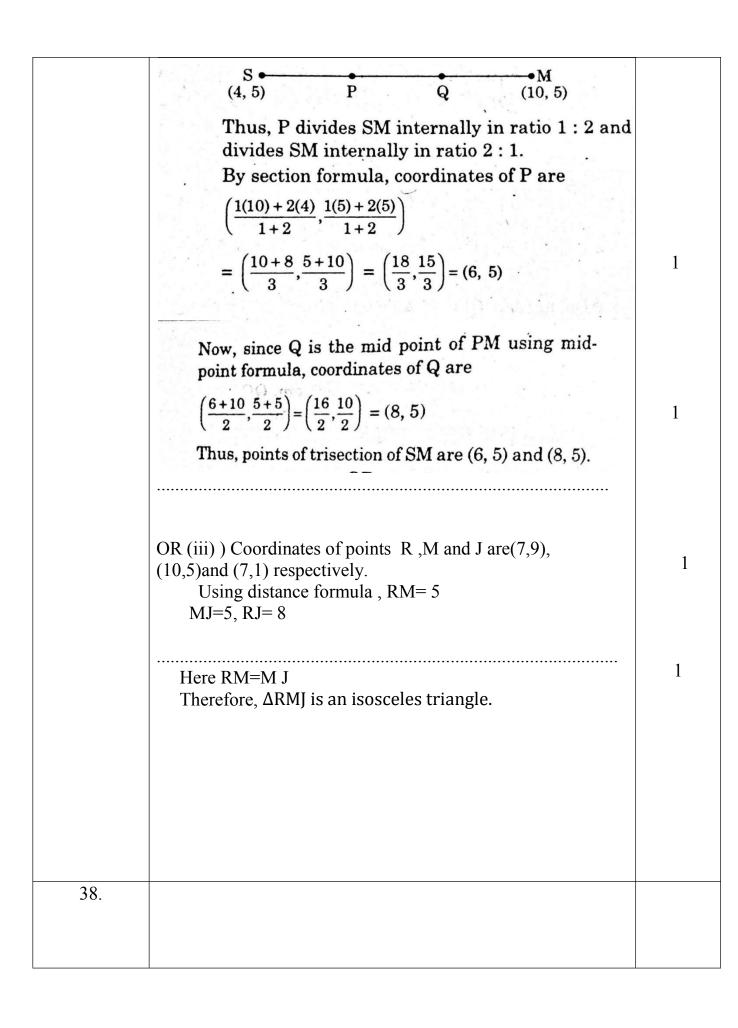
Frequency (f) of median class = 6

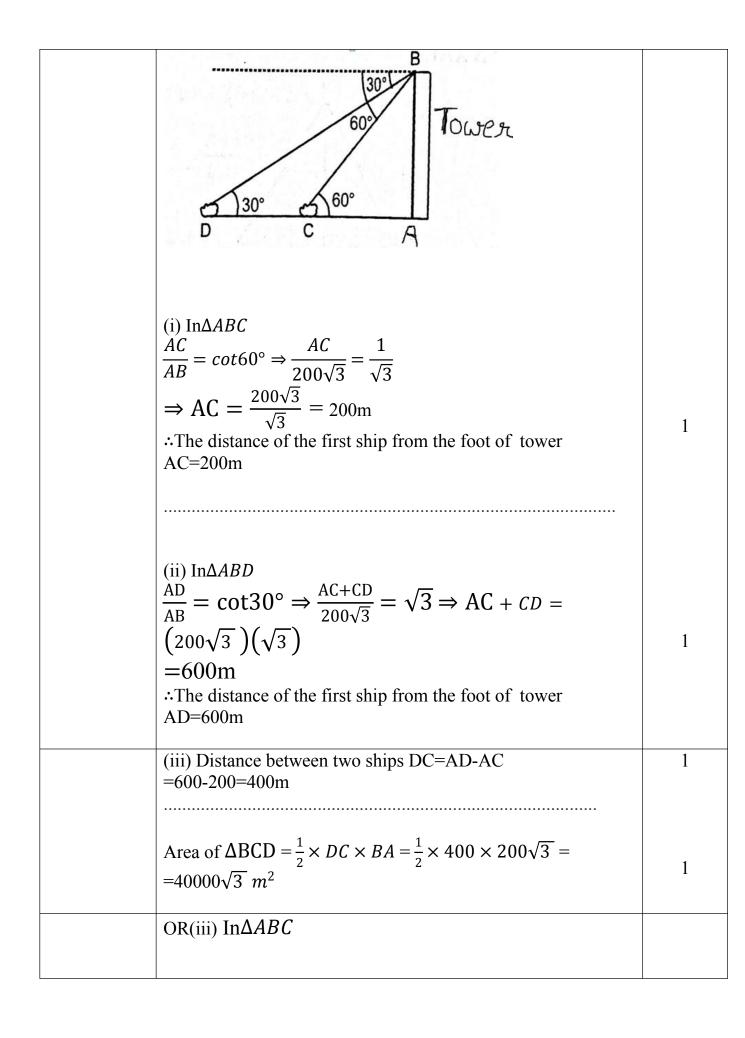
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1

| | Cumulative frequency (cf) of class preceding the median class = 13 | 1 |
|-----|--|---|
| | Class size (h) = 5 Median = $l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$ | 1 |
| | =55 + $\frac{15-13}{6}$ × 5 =55 + $\frac{10}{6}$ = 56.67 Therefore, median weight is 56.67 kg. | 1 |
| | SECTION E | |
| 36. | (i) $a = First term = 51 secs$ reduce time daily by 2secs d = -2 last term $a_n = 31$ a+(n-1)d = 31 31 = 51 + (n-1)(-2) 10 = n - 1 n = 11 11 Terms | |
| | the minimum number of days he needs to practice till his goal is achieved= 11 51, 49, 47, 45, 43, 41, 39, 37, 35, 33, 31 | 1 |
| | (ii) Because Veer need to practice. Because of his practice, The timing required to cover the distance can be reduced. | |
| | The given situation can be expressed in an arithmetic progression (AP), where the terms decrease by 2 seconds each day. Thus, the AP will be 51, 49, 47 | 1 |
| | (iii) | |

| $a_n=2n+3$ | |
|---|---|
| $a_1 = 2 \times 1 + 3 = 5$ | |
| $a_2=2\times 2 + 3 = 7$ | |
| $a_3=2\times 3 + 3 = 9$ | |
| $a_4=2\times 4 + 3 = 11$ | 1 |
| A.P. = 5,7,9,11 d = 7-5=2 | 1 |
| OR (iii) | |
| Since $2x,x+10,3x+2$ are three consecutive terms are in AP. $\therefore (x+10) - 2x = (3x+2) - (x+10)$ $\Rightarrow 10-x=2x-8$ | 1 |
| $\Rightarrow 18 = 3x$ $\Rightarrow x = 6$ | 1 |
| (i)) Revti' position is at (7,9) Sheela's position is at (4,5) | 1 |
| (ii)) $RJ = \sqrt{(7-7)^2 + (1-9)^2} = \sqrt{(0)^2 + (-8)^2} = \sqrt{64} = 8$ units | 1 |
| (iii)) Here SP= PQ =QM | |
| | |
| | a ₁ =2× 1 + 3 = 5 a ₂ =2× 2 + 3 = 7 a ₃ =2× 3 + 3 = 9 a ₄ =2× 4 + 3 = 11 |





| $\frac{200}{BC} = \frac{1}{2} \implies BC = 400 \text{ m}$ Perimeter of $\triangle ABC = AB + BC + AC$ $= 200\sqrt{3} + 400 + 200 = 600 + 200\sqrt{3}$ $= 200(3 + \sqrt{3}) \text{ m}$ | $\frac{AC}{BC} = \cos 60^{\circ} \Rightarrow$ | 1 |
|--|--|---|
| $= 200\sqrt{3} + 400 + 200 = 600 + 200\sqrt{3}$ | $\frac{200}{BC} = \frac{1}{2} \implies BC = 400 \text{ m}$ | |
| | $= 200\sqrt{3} + 400 + 200 = 600 + 200\sqrt{3}$ | 1 |