

# BSEH Practice Paper (March 2024)

(2023-24)

## Marking Scheme Model Question Paper

**SET-A**  
**CODE: 835**

**MATHEMATICS**

⇒ Important Instructions: • All answers provided in the Marking scheme are SUGGESTIVE  
• Examiners are requested to accept all possible alternative correct answer(s).

### SECTION – A (1Mark × 20Q)

Q. No.	EXPECTED ANSWERS	Marks
Question 1.	Let R be the relation in the set N given by $R = \{(a, b) : a = b - 2, b > 6\}$ . Choose the correct answer.	
<b>Solution:</b>	<b>(C) <math>(6, 8) \in R</math></b>	1
Question 2.	$\tan^{-1}\left(\tan \frac{7\pi}{6}\right)$ is equal to:	
<b>Solution:</b>	<b>(B) <math>\frac{\pi}{6}</math></b>	1
Question 3.	If $A = \begin{bmatrix} \tan \theta & \cot \theta \\ -\cot \theta & \tan \theta \end{bmatrix}$ , $0 < \theta < \frac{\pi}{2}$ and $A + A' = 2I$ , then the value of $\theta$ is:	
<b>Solution:</b>	<b>(A) <math>\frac{\pi}{4}</math></b>	1
Question 4.	If a matrix A is both symmetric and skew symmetric, then	
<b>Solution:</b>	<b>(B) A is a zero matrix</b>	1
Question 5.	If the vertices of a triangle are (1, 0), (6, 0) and (4, 3), then by using determinants its area is	
<b>Solution:</b>	<b>(C) <math>\frac{15}{2}</math></b>	1
Question 6.	If $y = x \cdot \log x$ , then $\frac{d^2y}{dx^2}$ is equal to:	
<b>Solution:</b>	<b>(A) <math>\frac{1}{x}</math></b>	1
Question 7.	The antiderivative of $\left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)$ equals:	
<b>Solution:</b>	<b>(C) <math>\frac{2}{3}x^{\frac{3}{2}} + 2x^{\frac{1}{2}} + C</math></b>	1
Question 8.	$\int e^x \left(\frac{1}{x} - \frac{1}{x^2}\right) dx$ equals:	
<b>Solution:</b>	<b>(B) <math>\frac{1}{x} e^x + C</math></b>	1
Question 9.	The value of $\int_{-1}^1 x^5 dx$ is	
<b>Solution:</b>	<b>(C) 0</b>	1
Question 10.	The order of the differential equation $2x^2 \frac{d^2y}{dx^2} - 3 \frac{dy}{dx} + y = 0$ is :	
<b>Solution:</b>	<b>(A) 2</b>	1
Question 11.	Which substitution can solve a homogeneous differential equation of the form $\frac{dx}{dy} = h\left(\frac{x}{y}\right)$ ?	
<b>Solution:</b>	<b>Put <math>x = vy</math></b>	1
Question 12.	The function $f(x) = \begin{cases} \sin x - \cos x, & \text{if } x \neq 0 \\ k, & \text{if } x = 0 \end{cases}$ is continuous at $x = 0$ , then find the value of k.	
<b>Solution:</b>	$\lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} (\sin x - \cos x)$ $= 0 - 1$ $= -1$ <p>Since <math>f(x)</math> is continuous at <math>x = 0</math></p> $\therefore \lim_{x \rightarrow 0} f(x) = f(0)$ $\Rightarrow -1 = k$	1
Question 13.	If a line has the direction ratios 2, -1, -2, then what are its direction cosines?	
<b>Solution:</b>	$\frac{2}{\sqrt{2^2+(-1)^2+(-2)^2}}, \frac{-1}{\sqrt{2^2+(-1)^2+(-2)^2}}, \frac{-2}{\sqrt{2^2+(-1)^2+(-2)^2}}$	1







**SECTION – C (3Marks × 8Q)**

	<b>SECTION – C (3Marks × 8Q)</b>	
<b>Question 26.</b>	Let $A = \mathbf{R} - \{3\}$ and $B = \mathbf{R} - \{1\}$ . Consider the function $f : A \rightarrow B$ defined by $f(x) = \left(\frac{x-2}{x-3}\right)$ . Is $f$ one one and onto? Justify your answer.	
<b>Solution:</b>	<p><math>A = \mathbf{R} - \{3\}</math> and <math>B = \mathbf{R} - \{1\}</math>  <math>f : A \rightarrow B</math> defined by <math>f(x) = (x - 2) / (x - 3)</math>  Let <math>(x, y) \in A</math> then  <math>f(x) = \frac{(x-2)}{(x-3)}</math> and <math>f(y) = \frac{(y-2)}{(y-3)}</math></p> <p>For <math>f(x) = f(y)</math>  <math>\frac{(x-2)}{(x-3)} = \frac{(y-2)}{(y-3)}</math>  <math>(x-2)(y-3) = (y-2)(x-3)</math>  <math>xy - 3x - 2y + 6 = xy - 3y - 2x + 6</math>  <math>-3x - 2y = -3y - 2x</math>  <math>-3x + 2x = -3y + 2y</math>  <math>-x = -y</math>  <math>x = y</math>  Therefore, <math>f</math> is a one-one function.</p> <p>Again, <math>y = f(x) = \frac{(x-2)}{(x-3)}</math>  <math>y = \frac{(x-2)}{(x-3)}</math>  <math>y(x-3) = x-2</math>  <math>xy - 3y = x-2</math>  <math>x(y-1) = 3y-2</math></p> <p>or <math>x = \frac{(3y-2)}{(y-1)}</math></p> <p>Now, <math>f\left(\frac{3y-2}{y-1}\right) =</math>  <math>\Rightarrow \frac{\frac{3y-2}{y-1} - 2}{\frac{3y-2}{y-1} - 3} = y</math>  <math>f(x) = y</math></p> <p>Therefore, <math>f</math> is onto function.</p>	<p align="center"><math>\frac{1}{2}</math></p> <p align="center">1</p> <p align="center"><math>\frac{1}{2}</math></p> <p align="center">1</p>
<b>OR Question 26.</b>	$\tan \frac{1}{2} \left[ \sin^{-1} \frac{2x}{1+x^2} + \cos^{-1} \frac{1-y^2}{1+y^2} \right]$ , $ x  < 1$ , $y > 0$ and $xy < 1$	
<b>Solution:</b>	<p>Put <math>x = \tan\theta</math> and <math>y = \tan\phi</math>, we have</p> $\tan \frac{1}{2} \left[ \sin^{-1} \left( \frac{2 \tan \theta}{1 + \tan^2 \theta} \right) + \cos^{-1} \left( \frac{1 - \tan^2 \phi}{1 + \tan^2 \phi} \right) \right]$ $= \tan \frac{1}{2} \left[ \sin^{-1} \sin 2\theta + \cos^{-1} \cos 2\phi \right]$ $= \tan \frac{1}{2} [2\theta + 2\phi]$ $= \tan(\theta + \phi)$ $= \frac{\tan \theta + \tan \phi}{1 - \tan \theta \tan \phi}$	<p align="center"><math>\frac{1}{2}</math></p> <p align="center"><math>1\frac{1}{2}</math></p> <p align="center">1</p>









Find the inverse of matrix:

Cofactors of matrix:

$$A_{11} = 0, \quad A_{12} = 2, \quad A_{13} = 1$$

$$A_{21} = -1, \quad A_{22} = -9, \quad A_{23} = -5$$

$$A_{31} = 2, \quad A_{32} = 23, \quad A_{33} = 13$$

$$\text{adj.}A = \begin{bmatrix} 0 & -1 & 2 \\ 2 & -9 & 23 \\ 1 & -5 & 13 \end{bmatrix}$$

So,

$$A^{-1} = \frac{1}{-1} \begin{bmatrix} 0 & -1 & 2 \\ 2 & -9 & 23 \\ 1 & -5 & 13 \end{bmatrix} = \begin{bmatrix} 0 & 1 & -2 \\ -2 & 9 & -23 \\ -1 & 5 & -13 \end{bmatrix}$$

Now, matrix of equations can be written as:  $AX=B$

$$\begin{bmatrix} 2 & -3 & 5 \\ 3 & 2 & -4 \\ 1 & 1 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 11 \\ -5 \\ -3 \end{bmatrix}$$

And,  $X = A^{-1} B$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 & 1 & -2 \\ -2 & 9 & -23 \\ -1 & 5 & -13 \end{bmatrix} \begin{bmatrix} 11 \\ -5 \\ -3 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

Therefore,  $x = 1$ ,  $y = 2$  and  $z = 3$ .

$\frac{1}{2}$

1

$\frac{1}{2}$

**Question 33.**

Find the shortest distance between the lines  $l_1$  and  $l_2$  whose vector equations are

$$\vec{r} = \hat{i} + \hat{j} + \lambda(2\hat{i} - \hat{j} + \hat{k})$$

$$\text{and } \vec{r} = 2\hat{i} + \hat{j} - \hat{k} + \mu(3\hat{i} - 5\hat{j} + 2\hat{k})$$

**Solution:**

$$\vec{r} = \hat{i} + \hat{j} + \lambda(2\hat{i} - \hat{j} + \hat{k}) \quad \dots(1)$$

$$\text{and } \vec{r} = 2\hat{i} + \hat{j} - \hat{k} + \mu(3\hat{i} - 5\hat{j} + 2\hat{k}) \quad \dots(2)$$

Comparing (1) and (2) with  $\vec{r} = \vec{a}_1 + \lambda \vec{b}_1$  and  $\vec{r} = \vec{a}_2 + \mu \vec{b}_2$  respectively,

we get

$$\vec{a}_1 = \hat{i} + \hat{j}, \quad \text{and } \vec{b}_1 = 2\hat{i} - \hat{j} + \hat{k}$$

$$\vec{a}_2 = 2\hat{i} + \hat{j} - \hat{k} \quad \text{and } \vec{b}_2 = 3\hat{i} - 5\hat{j} + 2\hat{k}$$

Therefore

$$\vec{a}_2 - \vec{a}_1 = \hat{i} - \hat{k}$$

and

$$\vec{b}_1 \times \vec{b}_2 = (2\hat{i} - \hat{j} + \hat{k}) \times (3\hat{i} - 5\hat{j} + 2\hat{k})$$

1

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	$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & -1 & 1 \\ 3 & -5 & 2 \end{vmatrix} = 3\hat{i} - \hat{j} - 7\hat{k}$ $ \vec{b}_1 \times \vec{b}_2  = \sqrt{9 + 1 + 49} = \sqrt{59}$ <p>Hence, the shortest distance between the given lines is given by</p> $D = \frac{ (\vec{a}_2 - \vec{a}_1) \cdot (\vec{b}_1 \times \vec{b}_2) }{ \vec{b}_1 \times \vec{b}_2 } = \frac{ 3 - 0 + 7 }{\sqrt{59}} = \frac{10}{\sqrt{59}}$	$\frac{1}{2}$  1  1
<b>OR Question 33.</b>	<p>Find the vector equation of the line passing through the point (1,2,-4) and perpendicular to the two lines :</p> $\frac{x-8}{3} = \frac{y+19}{-16} = \frac{z-10}{7} \quad \text{and} \quad \frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}$	
<b>Solution:</b>	<p>The vector equation of a line passing through a point with position vector <math>\vec{a}</math> and parallel to <math>\vec{b}</math> is <math>\vec{r} = \vec{a} + \lambda \vec{b}</math>. It is given that, the line passes through (1, 2, -4)</p> <p>So, <math>\vec{a} = 1\hat{i} + 2\hat{j} - 4\hat{k}</math></p> <p>Given lines are <math>\frac{x-8}{3} = \frac{y+19}{-16} = \frac{z-10}{7}</math> and <math>\frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}</math></p> <p>It is also given that, line is perpendicular to both given lines. So we can say that the line is perpendicular to both parallel vectors of two given lines.</p> <p>We know that, <math>\vec{a} \times \vec{b}</math> is perpendicular to both <math>\vec{a}</math> &amp; <math>\vec{b}</math>, so let <math>\vec{b}</math> is cross product of parallel vectors of both lines i.e. <math>\vec{b} = \vec{b}_1 \times \vec{b}_2</math>  where <math>\vec{b}_1 = 3\hat{i} - 16\hat{j} + 7\hat{k}</math> and <math>\vec{b}_2 = 3\hat{i} - 8\hat{j} - 5\hat{k}</math></p> <p>and Required Normal</p> $\vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -16 & 7 \\ 3 & 8 & -5 \end{vmatrix}$ $= \hat{i}(80 - 56) - \hat{j}(-15 - 21) + \hat{k}(24 + 48)$ $\vec{b} = 24\hat{i} + 36\hat{j} + 72\hat{k}$ <p>Now, by substituting the value of <math>\vec{a}</math> &amp; <math>\vec{b}</math> in the formula <math>\vec{r} = \vec{a} + \lambda \vec{b}</math>, we get</p> $\vec{r} = (1\hat{i} + 2\hat{j} - 4\hat{k}) + \lambda(24\hat{i} + 36\hat{j} + 72\hat{k})$	1  2  1
<b>Question 34.</b>	<p>Find the area of the region bounded by the curve <math>y^2 = x</math> and the lines <math>x = 1</math>, <math>x = 4</math> and x-axis in the first quadrant.</p>	
<b>Solution:</b>	<p>Equation of the curve is <math>y^2 = x</math>.  It is a rightward parabola having vertex at origin and symmetrical about x-axis. <math>x = 1</math> and <math>x = 4</math> are two straight lines parallel to y-axis.  <math>y = \sqrt{x}</math> ....(1) <math>x = 1</math> and <math>x = 4</math></p> <p>Points of intersections of given curves  At <math>x = 1</math>, <math>y = \sqrt{1} = \pm 1</math> points are (1, 1) (1, -1)  At <math>x = 4</math>, <math>y = \sqrt{4} = \pm 2</math> points are (4, 2) (4, -2)  <math>\therefore</math> points in first quadrant A(1, 1) B(4, 2) C(4, 0), D(1, 0)</p> <p>Make a rough hand sketch of given curves by taking some corresponding values</p>	$\frac{1}{2}$

of x and y.

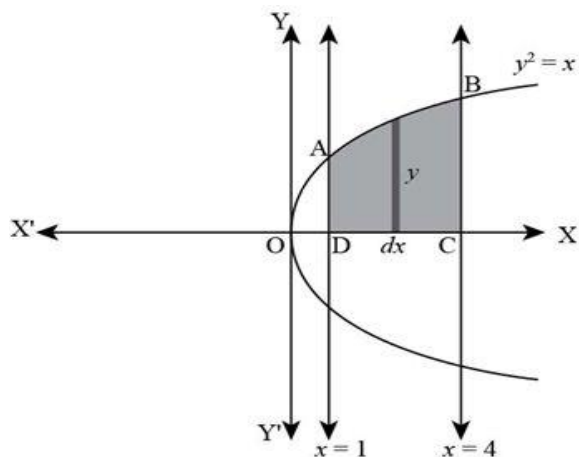


Figure (1)

Required area is shaded region ABCD:

$$| \int_1^4 y \, dx | = | \int_1^4 \sqrt{x} \, dx | \quad [ \text{From equation (1)} ]$$

$$= | \int_1^4 x^{1/2} \, dx |$$

$$| \frac{x^{3/2}}{3/2} |_1^4$$

$$= \frac{2}{3} | (4^{3/2} - 1^{3/2}) |$$

$$= \frac{2}{3} | (8 - 1) | = \frac{2}{3} (7) = \frac{14}{3} \text{ sq. units}$$

1

$1\frac{1}{2}$

1

**OR**  
**Question 34.**

Find the area of the region bounded by the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$

**Solution:**

$$\text{Here } \frac{x^2}{16} + \frac{y^2}{9} = 1 \quad \dots(1)$$

It is a horizontal ellipse having center at origin and is symmetrical about both axes (if we change y to -y or x to -x, equation remain same).

Standard equation of an ellipse is  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$

By comparing, a = 4 and b = 3

From equation (1)

$$\Rightarrow y^2 = \frac{9}{16} (16 - x^2)$$

$$\Rightarrow y = \frac{3}{4} \sqrt{16 - x^2} \quad \dots(2)$$

Points of Intersections of ellipse (1) with x-axis (y = 0)

Put y = 0 in equation (1), we have

$$x^2/16 = 1$$

$$\Rightarrow x^2 = 16$$

$$\Rightarrow x = \pm 4$$

Therefore, Intersections of ellipse(1) with x-axis are (0, 4) and (0, -4).

Now again,

Points of Intersections of ellipse (1) with y-axis (x = 0)

Putting x = 0 in equation (1),  $y^2/9 = 1$

$$\Rightarrow y^2 = 9$$

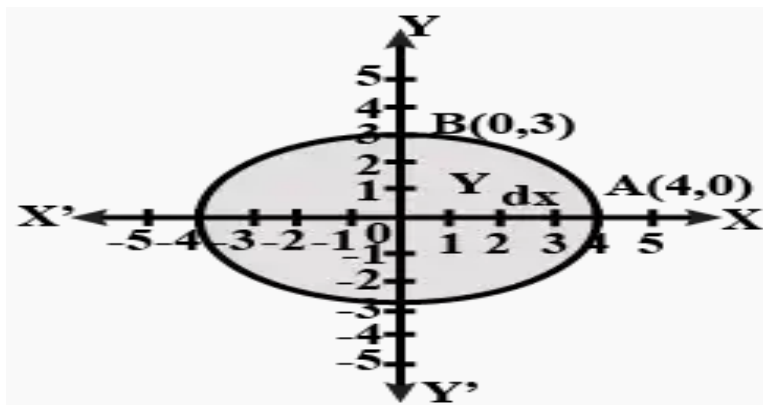
$$\Rightarrow y = \pm 3.$$

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1

Therefore, Intersections of ellipse (1) with y-axis are (0, 3) and (0,-3).

for arc of ellipse in first quadrant.



Now,

Area of region bounded by ellipse (1)

Total shaded area = 4 x Area OAB of ellipse in first quadrant

$$= 4 \int_0^4 y \cdot dx \quad [ \because \text{at end B of arc AB of ellipse: } x=0 \text{ and at end A of arc AB; } x=4 ]$$

$$= 4 \int_0^4 \frac{3}{4} \sqrt{16 - x^2} \cdot dx = 3 \int_0^4 \sqrt{4^2 - x^2} \cdot dx$$

$$= 3 \left[ \frac{x}{2} \sqrt{4^2 - x^2} + \frac{4^2}{2} \sin^{-1} \frac{x}{4} \right]_0^4 \quad [ \because \int \sqrt{a^2 - x^2} dx = \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} ]$$

$$3 \left[ \left( \frac{4}{2} \sqrt{16 - 16} + 8 \sin^{-1} 1 \right) - \left( 0 + 8 \sin^{-1} 0 \right) \right] = 3 [ 0 + (8\pi/2) ]$$

$$= 3(4\pi) = 12\pi \text{ sq. units}$$

1

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1

**Question 35.**

Solve the following problem graphically:

Minimise and Maximise  $Z = 3x + 9y$

Subject to the constraints:  $x + 3y \leq 60$

$$x + y \geq 10$$

$$x \leq y$$

$$x \geq 0, y \geq 0$$

**Solution:**

$$Z = 3x + 9y. \quad (1)$$

$$x + 3y \leq 60 \quad (2)$$

$$x + y \geq 10. \quad (3)$$

$$x \geq y \quad (4)$$

$$x \geq 0, y \geq 0 \quad (5)$$

First of all, let us graph the feasible region of the system of linear inequalities (2) to (5).

$$\text{Let } Z = 3x + 9y \quad \dots(1)$$

Converting inequalities to equalities

$$x + 3y = 60$$

X	0	60
Y	20	0

Points are (0, 20), (60,0)

Now put (0, 0) in inequation (2),

we find  $0 \leq 60$ , which is true.  
Therefore area lies towards the origin from this line.

$$x + y = 10$$

x	0	10
y	10	0

Points are (0, 10), (10, 0)

Now put (0, 0) in inequation (3),  
we find  $0 \geq 10$ , which is False.

Therefore area lies away from the origin from this line.

$$x - y = 0$$

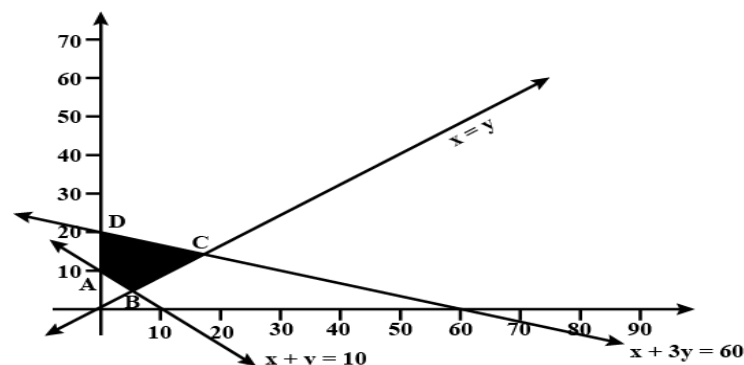
X	0	10	20
y	0	10	20

Points are (0,0),(10,10),(20,20)

Now put (1, 0) in inequation (4),  
we find  $1 \geq 0$ , which is false.

Therefore area lies away from the (1, 0) from this line.

Plot the graph for the set of points



To find maximum and minimum

The feasible region ABCD is shown in the figure. Note that the region is bounded. The coordinates of the corner points A, B, C and D are (0, 10), (5, 5), (15, 15) and (0, 20) respectively.

Corner Point	Corresponding Value of $Z = 3x + 9y$
A (0, 10)	90
B (5, 5)	<b>60 ← Minimum</b>
C (15, 15)	<b>180 ← Maximum</b>
D (0, 20)	<b>180 (Multiple optimal solutions)</b>

We now find the minimum and maximum value of Z.

From the table, we find that the minimum value of Z is 60 at the point B (5, 5) of the feasible region.

The maximum value of Z on the feasible region occurs at the two corner points C (15, 15) and D (0, 20) and it is 180 in each case.

**SECTION – E ( 4Marks × 3Q)**

	<b>SECTION – E ( 4Marks × 3Q)</b>	
<b>Question 36.</b>	<p>The proportion of a river's energy that can be obtained from an undershot water wheel is <math>E(x) = 2x^3 - 4x^2 + 2x</math>, units where <math>x</math> is the speed of the water wheel relative to the speed of the river.</p> <p><i>Based on the above information answer the following :</i></p> <p>(i) Find the maximum value of <math>E(x)</math> in the interval <math>[0, 1]</math>. (2)</p> <p>(ii) What is the speed of water wheel for maximum value of <math>E(x)</math>? (1)</p> <p>(iii) Does your answer agree with Mill wrights rule that the speed of wheel should be about one-third of the speed of the river? (1)</p>	
<b>Solution:</b>	<p>(i) We have, <math>E(x) = 2x^3 - 4x^2 + 2x</math> ... (1)</p> <p style="padding-left: 20px;">Differentiating equation (1) w.r.t. <math>x</math></p> <p style="padding-left: 40px;"><math>E'(x) = 6x^2 - 8x + 2</math> ... (2)</p> <p>For maximum or minimum value of <math>E(x)</math>, <math>E'(x) = 0</math> we have</p> <p><math>6x^2 - 8x + 2 = 0</math></p> <p><math>3x^2 - 4x + 1 = 0</math></p> <p><math>(3x - 1)(x - 1) = 0</math></p> <p>i.e. <math>x = 1/3, x = 1</math></p> <p style="padding-left: 20px;">Differentiating equation (2) w.r.t. <math>x</math></p> <p><math>E''(x) = 12x - 8</math></p> <p>Now ,</p> <p>At <math>x = 1</math>      <math>E''(x) = 12(1) - 8 = 4 = +ve</math></p> <p>At <math>x = 1/3</math>    <math>E''(x) = 12(1/3) - 8 = -4 = -ve</math></p> <p><math>\Rightarrow E(x)</math> has maximum value at <math>x = 1/3</math></p> <p>Maximum value = <math>E(1/3) = 2(1/3)^3 - 4(1/3)^2 + 2(1/3)</math>  <math>= 2/27 - 4/9 + 2/3 = 8/27</math></p>	1
	(ii) Speed for the Maximum value of $E(x)$ is $\frac{1}{3}$ units.	1
	(iii) Yes	1
<b>Question 37.</b>	<p>A linear differential equation is of the form <math>\frac{dy}{dx} + Py = Q</math>, where <math>P, Q</math> are functions of <math>x</math>, then such equation is known as linear differential equation. Its solution is given by <math>y \cdot (I.F.) = \int Q(I.F.) dx + c</math>, where <math>I.F.</math> (Integrating Factor) = <math>e^{\int P dx}</math></p> <p>Now, suppose the given equation is <math>x dy + y dx = x^3 dx</math></p> <p><i>Based on the above information, answer the following questions:</i></p> <p>(i) What are the values of <math>P</math> and <math>Q</math> respectively? (1)</p> <p>(ii) What is the value of <math>I.F.</math>? (1)</p> <p>(iii) Find the Solution of given equation. (2)</p>	

<p><b>Solution:</b></p>	<p>(i) Given equation is <math>x \cdot dy + y \cdot dx = x^3 dx</math>  Dividing on both side by <math>dx</math>, we have</p> $x \frac{dy}{dx} + y = x^3$ $\frac{dy}{dx} + \frac{1}{x} y = x^2$ $\Rightarrow P = \frac{1}{x}, Q = x^2$	<p>1</p>
	<p>(ii) I.F.( Integrating Factor) = <math>e^{\int P dx}</math></p> $= e^{\int \frac{1}{x} dx}$ $= e^{\log x}$ $= x$	<p>1</p>
	<p>(iii) Solution of given equation is</p> $y \cdot (\text{I.F.}) = \int Q(\text{I.F.}) dx + c$ $y(x) = \int x^2(x) dx + c$ $xy = \int x^3 dx + c$ $xy = \frac{x^4}{4} + c$	<p>2</p>
<p><b>Question 38.</b></p>	<p>Ratna has two boxes I and II. Box I contains 3 red and 6 black balls. Box II contains 5 red and 5 black balls. Her friend Shivani selects one of the two boxes randomly and draws a ball out of it. The ball drawn by Shivani is found to be red. Let <math>E_1</math>, <math>E_2</math> and <math>A</math> denote the following events:  <math>E_1</math> : Box I is selected by Shiavni.  <math>E_2</math> : Box II is selected by Shiavni.  <math>A</math> : Red ball is drawn by Shivani.</p> <p>(a) Find <math>P(E_1)</math> and <math>P(E_2)</math> (1)  (b) Find <math>P(A E_1)</math> and <math>P(A E_2)</math> (1)  (c) Find <math>P(E_2   A)</math> (2)</p>	
<p><b>Solution:</b></p>	<p>(a) <math>P(E_1)</math> : Probability of selecting Box I by Shiavni = <math>\frac{1}{2}</math>  <math>P(E_1)</math> : Probability of selecting Box I by Shiavni = <math>\frac{1}{2}</math></p>	<p>1</p>
	<p>(b) <math>P(A E_1)</math> = Probability of selecting a red ball when box I has been already selected = <math>\frac{3}{9}</math>  <math>P(A E_2)</math> = Probability of selecting a red ball when box II has been already selected = <math>\frac{5}{10}</math></p>	<p>1</p>
	<p>(c) <math>P(E_2   A)</math> = Probability that a red ball is drawn from the box II</p> <p>By Bayes' Theorem</p> $P(E_2   A) = \frac{P(E_2) \cdot P(A E_2)}{P(E_1) \cdot P(A E_1) + P(E_2) \cdot P(A E_2)}$	

$$P(E_2 | A) = \frac{\frac{1}{2} \cdot \frac{5}{10}}{\frac{1}{2} \cdot \frac{3}{9} + \frac{1}{2} \cdot \frac{5}{10}}$$

$$P(E_2 | A) = \frac{\frac{1}{4}}{\frac{1}{6} + \frac{1}{4}}$$

$$P(E_2 | A) = \frac{\frac{1}{4}}{\frac{4+6}{24}} = \frac{1}{4} \times \frac{24}{10} = \frac{3}{5}$$

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